

## 9 Trigonometric functions

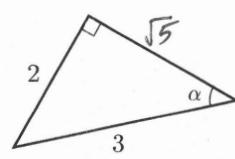
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- 1 For the right triangle in the figure below, find the sine, cosine, and tangent of the angle  $\alpha$ .

a)  $\sin \alpha = \frac{2}{3}$

b)  $\cos \alpha = \frac{\sqrt{5}}{3}$

c)  $\tan \alpha = \frac{2}{\sqrt{5}} = \frac{2\sqrt{5}}{5}$



- 2 Express the following expressions in terms of  $\sin \theta$ ,  $\cos \theta$ ,  $\tan \theta$ .

a)  $\sin(90^\circ - \theta) = \cos \theta$

b)  $\cos(90^\circ - \theta) = \sin \theta$

c)  $\tan(90^\circ - \theta) = \frac{1}{\tan \theta}$

- 3 Assuming  $\sin \theta = \frac{4}{5}$  and  $0^\circ < \theta < 90^\circ$ , find the following values.

a)  $\cos \theta = \frac{3}{5}$

b)  $\tan \theta = \frac{4}{3}$

- 4 Convert the following angles to radians.

a)  $90^\circ = \frac{\pi}{2}$

b)  $120^\circ = \frac{2\pi}{3}$

c)  $210^\circ = \frac{7\pi}{6}$

d)  $225^\circ = \frac{5\pi}{4}$

e)  $240^\circ = \frac{4\pi}{3}$

f)  $330^\circ = \frac{11\pi}{6}$

- 5 Convert each radian measure to degrees.

a)  $\frac{\pi}{6} = 30^\circ$

b)  $\frac{\pi}{3} = 60^\circ$

c)  $\frac{3\pi}{4} = 135^\circ$

d)  $\frac{4\pi}{3} = 240^\circ$

e)  $\frac{3\pi}{2} = 270^\circ$

f)  $\frac{7\pi}{4} = 315^\circ$

- 6 Complete the following table.

$\theta$	$\frac{7}{6}\pi$	$\frac{7}{4}\pi$	$\frac{5}{4}\pi$	$-\frac{\pi}{3}$	$-\pi$
$\sin \theta$	$-\frac{1}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{3}}{2}$	0
$\cos \theta$	$-\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$-\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	-1

- 7 Express the following expressions in terms of  $\sin \theta$ ,  $\cos \theta$ ,  $\tan \theta$ .

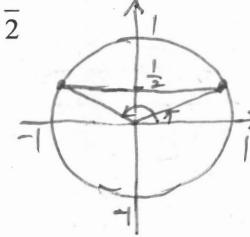
a)  $\sin(-\theta) = -\sin \theta$

b)  $\cos(-\theta) = \cos \theta$

c)  $\tan(-\theta) = -\tan \theta$

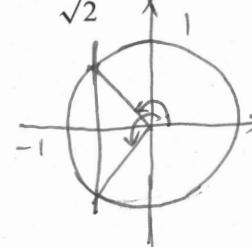
- 8 Solve each of the following equations for  $\theta$  assuming  $0 \leq \theta < 2\pi$ .

a)  $\sin \theta = \frac{1}{2}$



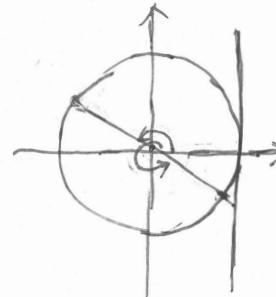
$\theta = \frac{\pi}{6}, \frac{5\pi}{6}$

b)  $\cos \theta = -\frac{1}{\sqrt{2}}$



$\theta = \frac{3\pi}{4}, \frac{5\pi}{4}$

c)  $\tan \theta = -\frac{1}{\sqrt{3}}$



$\theta = \frac{5\pi}{6}, \frac{11\pi}{6}$